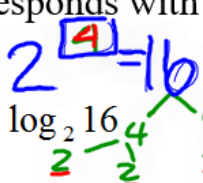
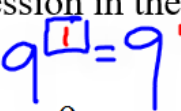
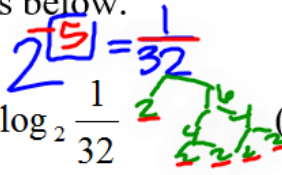
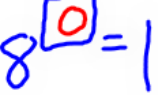
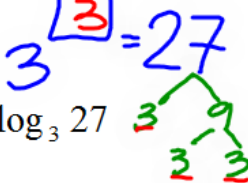


Test 2 Review

In CLASS

**Sec 3 Test 2 Review
Logarithmic Functions**

1. Put these logarithmic expressions in order from smallest to largest by writing the *letter* that corresponds with each expression in the spaces below.

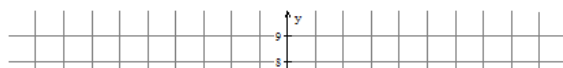
(A) $\log_2 16$  (B) $\log_9 9$  (C) $\log_2 \frac{1}{32}$  (D) $\log_8 1$  (E) $\log_3 27$ 

$\frac{C}{-5}$
 $\frac{D}{0}$
 $\frac{B}{1}$
 $\frac{E}{3}$
 $\frac{A}{4}$

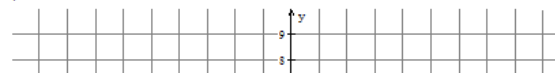
Smallest \longrightarrow Largest

Graph the following functions. Mark and label at least two points on each graph.

2a. $f(x) = 3^x$



b. $f(x) = 3^x - 3$



2a. $f(x) = 3^x$

x	3^x
0	$3^0 = 1$
1	$3^1 = 3$
2	$3^2 = 9$
3	$3^3 = 27$

c. Describe the Translation:
down 3

b. $f(x) = 3^x - 3$ down 3

x	$3^x - 3$
0	$3^0 - 3 = -2$
1	$3^1 - 3 = 0$
2	$3^2 - 3 = 6$

*outside = up & down (out, doubt rhymes)
* (inside) = to the OPPOSITE side, change happens to x.
left & right

3a. $f(x) = \log_3 x \leftrightarrow 3^y = x$

x	3^y	y
1	$3^0 = 1$	0
3	$3^1 = 3$	1
9	$3^2 = 9$	2

c. Describe the Translation:
left 2

b. $f(x) = \log_3(x+2)$ left 2

x	$3^y = x+2$	y
-1	$3^0 = x+2 \Rightarrow 0 = x+2 \Rightarrow x = -2$	0
1	$3^1 = x+2 \Rightarrow 1 = x+2 \Rightarrow x = -1$	1
7	$3^2 = x+2 \Rightarrow 9 = x+2 \Rightarrow x = 7$	2

short cut

long way

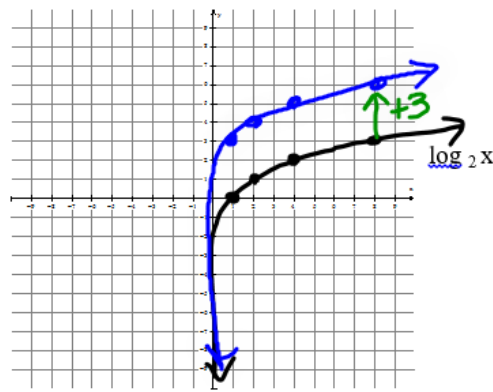
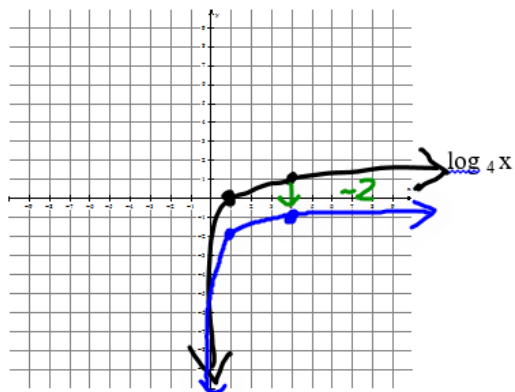
Graph Translations: *Use properties of logarithms to expand and simplify each expression completely then graph the translations, shifting ALL POINTS.*

Celia Gubler is signed in

4.a. $f(x) = \log_4 \frac{x}{16}$ 4² = 16
 = $\log_4 x - \log_4 16$

5.a. $f(x) = \log_2 (8x)$ 2³ = 8
 = $\log_2 8 + \log_2 x$

b. Describe the translation to $\log_4 x$ -2, down 2 b. Describe the translation to $\log_2 x$ +3, up 3



Use properties of logarithms to expand each expression completely.

6. $\log_7 (5x^2)$

7. $\log_2 \left(\frac{3a}{5} \right)$

Use properties of logarithms to expand each expression completely. *only. No decimals.*

6. $\log_7(5x^2)$
 $\log_7 5 + 2 \cdot \log_7 x^2$
 $\log_7 5 + 2 \cdot \log_7 x$

7. $\log_2\left(\frac{3a}{5}\right)$
 $\log_2 3 + \log_2 a - \log_2 5$

Evaluate the following logarithms. (Show factor tree)

2. $\log_{10} 10,000$
 $10^4 = 10000$
 Factor tree for 10000: 10000 → 100 × 100 → 10 × 10 × 10 × 10

3. $\log_3 \frac{1}{9}$
 $3^2 = 9$
 $\frac{1}{3^2} = \frac{1}{9}$

4. $\log_2 32$
 $2^5 = 32$
 Factor tree for 32: 32 → 4 × 8 → 2 × 2 × 2 × 2 × 2

Use $\log_4 5 \approx 1.2$ and $\log_4 3 \approx 0.8$, along with properties of logarithms, to evaluate the following. Show all of your steps. *Must re-write each question so that it is in multiples of 4, 5, 3, 1*

11. $\log_4 25$
 $2 \cdot \log_4 5^2$
 $2 \cdot (1.2) = 2.4$

12. $\log_4 \frac{1}{3} - \log_4 1 - \log_4 3$
 $\log_4 1 - \log_4 3$
 $0 - 0.8 = -0.8$

or 36
 $3 \cdot 12$
 $3 \cdot 4 \cdot 3$
 $3 \cdot 4 \cdot 3$
 don't have 2's.
 13. $\log_4 \frac{36}{5}$
 $\frac{4 \cdot 3^2}{5}$
 Uses 3, 4, 5

$\log_4 4 + 2 \cdot \log_4 3^2 - \log_4 5$
 $\log_4 4 + 2 \cdot \log_4 3 - \log_4 5$
 $1 + 2(0.8) - 1.2 = 1.4$

same idea as $3^2 = 3^2$

Solve the logarithmic equation for x. Show all of your work.

14. $\log_3(3x-2) - \log_3 7 = 0$ $+ \log_3 7$ $\log_3 7$ $\log_3 7$ $\log_2(5x-1) = 1$ $\log_2(3x-3)$

$$3x-2 = 7$$

$$3x = 9$$

$$x = 3$$

$$5x-1 = 3x-3$$

$$2x-1 = -3$$

$$2x = -2$$

$$x = -1$$

aaa bb
aaa bb

Simplify, show all of your work.

16. $(2a^3b^2)^2$

$$2^2(a^3)^2(b^2)^2$$

$$4a^6b^4$$

Find the INVERSE of each function:

19. $f(x) = 6x - 4$

17. $5^{2p-1} = 5^3$

$$2p-1 = 3$$

$$2p = 4$$

$$p = 2$$

18. $11(-6)^0$

$$11 \cdot 1 = 11$$

$3^{-1} = \frac{1}{3}$
 $3^0 = 1$
 $3^1 = 3$

Anything to the zero power = 1!

$-6^{-1} = -\frac{1}{6}$
 $-6^0 = 1$
 $-6^1 = -6$

Find the INVERSE of each function:

1. Switch $x \leftrightarrow y$ 2. Solve for y

19. $f(x) = 6x - 4$

$$x = 6y - 4$$

$$\frac{x+4}{6} = \frac{6y}{6}$$

$$\frac{x+4}{6} = y$$

$$\frac{x}{6} + \frac{4}{6} = y$$

20. $f(x) = \frac{y-3}{6}$

$$6 \cdot x = \frac{y-3}{6} \cdot 6$$

$$6x = \frac{y-3}{1}$$

$$6x + 3 = y$$

21. Given $f(x) = 3x + 11$ and $g(x) = \frac{x-11}{3}$. Show $f(g(x))$ and answer if they are inverses.

$$f(g(x)) = 3\left(\frac{x-11}{3}\right) + 11$$

$$x - 11 + 11$$

X INVERSES!

$f(x)$ $g(x)$ inside, replace x with the equation for $g(x)$.

*side note | what happens to x ?

$f(x) = 3x + 11$
 $g(x) = \frac{x-11}{3}$

$\cdot 3$ then $+11$
 -11 then $\div 3$ INVERSES Reverses!

Test 2 Review HOMEWORK

corresponds with each expression in the spaces below.

$5^2 = 25$
 $5^3 = 125$
 $5^3 = 125$
 $5^4 = 625$

$2^1 = 2$
~~(A) $\log_2 2$~~

$5^4 = 625$
~~(B) $\log_5 625$~~

$9^2 = 81$
~~(C) $\log_9 \frac{1}{81}$~~

$4^0 = 1$
~~(D) $\log_4 1$~~

$3^5 = 243$
~~(E) $\log_3 243$~~

C	D	A	B	E
-2	0	1	4 ~ 3..	5

Smallest \longrightarrow Largest

Graph the following functions. Mark and label at least two points on each graph.

2a. $f(x) = 3^x$

b. $f(x) = 3^x + 4$

c. Describe the Translation: _____

AGE 1 OF 3 206 WORDS
140%

2a. $f(x) = 3^x$

x	3^x
0	$3^0 = 1$
1	$3^1 = 3$
2	$3^2 = 9$
3	$3^3 = 27$

b. $f(x) = 3^x + 4$

c. Describe the Translation: **up 4**

3a. $f(x) = \log_3 x$

x	$\log_3 x$
1	0
3	1
9	2

b. $f(x) = \log_3(x-3) = 0 + 3$

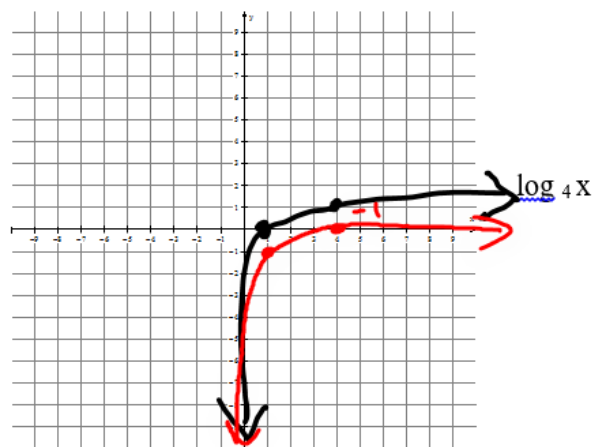
c. Describe the Translation: **right 3**

INVERSES, can switch x & y.

Graph Translations: Use properties of logarithms to **expand and** simply each expression completely then graph the translations, shifting ALL POINTS.

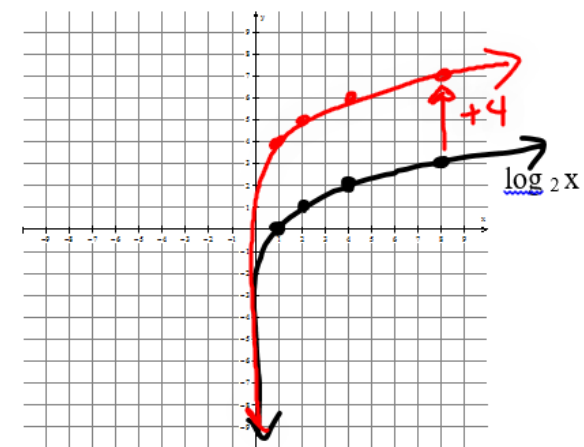
4.a. $f(x) = \log_4 \frac{x}{4}$ $\uparrow 4^1 = 4$
 $= \log_4 x - \log_4 4$

b. Describe the translation to $\log_4 x$ -1, down 1



5.a. $f(x) = \log_2 (16x)$ $\uparrow 2^4 = 16$
 $= \log_2 16 + \log_2 x$ $\begin{matrix} 4 \\ 2 \\ -2 \end{matrix}$

b. Describe the translation to $\log_2 x$ +4, up 4



Use properties of logarithms to expand each expression completely.

Use properties of logarithms to expand each expression completely.

6. $\log_7(8x^3)$
 $\log_7 8 + 3\log_7 x$

7. $\log_2\left(\frac{6x}{5}\right) - \log_2 6 + \log_2 x - \log_2 5$

Evaluate the following logarithms. (Show factor tree)

8. $\log_{10} 1000$

$10^3 = 1000$
 $\log_{10} 1000 = 3$

9. $\log_3 \frac{1}{81}$
 $3^4 = 81$
 $\log_3 \frac{1}{81} = -4$

10. $\log_4 64$

$4^3 = 64$
 $\log_4 64 = 3$

$4^0 = 1$
 $\log_4 1 = 0$
 $4^1 = 4$
 $\log_4 4 = 1$
 $4^2 = 16$
 $\log_4 16 = 2$
 $4^3 = 64$
 $\log_4 64 = 3$
 $4^4 = 256$
 $\log_4 256 = 4$

Use $\log_4 5 \approx 1.2$ and $\log_4 3 \approx 0.8$, along with properties of logarithms, to evaluate the following. Show all of your steps.

rewrite using multiples of 1, 3, 4, 5

~~EXPAND~~

11. $\log_4 15$
 $\log_4(3 \cdot 5)$
 $\log_4 3 + \log_4 5$
 $0.8 + 1.2 = 2$

12. $\log_4 \frac{1}{9}$
 $\log_4 3^{-2}$
 $-2 \cdot (\log_4 3)$
 $-2 \cdot (0.8) = -1.6$

13. $\log_4 \frac{45}{4}$
 $\log_4 3 + \log_4 5 - \log_4 4$
 $0.8 + 1.2 - 1 = 1.0$
 $1.6 + 1.2 - 1 = 1.8$

Solve the logarithmic equation for x. Show all of your work.

14. $\log_3(x+3) - \log_3 9 = 0 + \log_3 9$
 $\log_3(x+3) = \log_3 9$
 $x+3 = 9$
 $x = 6$

15. $\log_2(6x+2) = \log_2(4x+4)$
 $6x+2 = 4x+4$
 $-4x \quad -4x$
 $2x+2 = 4$
 $-2 \quad -2$
 $2x = 2$
 $x = 1$

• aaaaaa
 • aaaaaa
 • 3.3
 • bbb
 • bbb

Simplify, show all of your work.

16. $(3a^6b^3)^2$
 $3^2(a^6)^2(b^3)^2$
 $9a^{12}b^6$

17. $5^{3p-2} = 5^7$
 $3p-2 = 7$
 $+2 \quad +2$
 $3p = 9$
 $p = 3$

ANYTHING
 to the zero
 power
 = 1.

18. $25(8^0)$

$25 \cdot 1 = 25$

Find the INVERSE of each function:

Find the INVERSE of each function:

1. Switch x & y 2. Solve for y .

19. $f(x) = 7y - 2$

$$x = 7y - 2$$

$$+2 \quad +2$$

$$\frac{x+2}{7} = \frac{7y}{7}$$

$$\boxed{\frac{x+2}{7} = y} \quad \text{or} \quad \boxed{\frac{x}{7} + \frac{2}{7} = y}$$

20. $f(x) = \frac{y-5}{4}$

$$4 \cdot x = \frac{y-5}{4} \cdot 4$$

$$4x = \frac{y-5}{1}$$

$$+5 \quad +5$$

$$\boxed{4x + 5 = y}$$

21. Given $f(x) = 5x - 12$ and $g(x) = \frac{x+12}{5}$ Show $f(g(x))$ and answer if they are inverses.

$$f(x) = 5x - 12$$

$$f(g(x)) = 5\left(\frac{x+12}{5}\right) - 12$$

$$= \cancel{5} \cdot \cancel{x+12} - 12$$

$$= \boxed{x} \text{ INVERSES}$$

$f(x)$ $g(x)$ inside, replace x with equation $g(x)$.

* Notice what happens to x ?
 $f(x) = 5x - 12$ $\cdot 5$ then -12
 $g(x) = \frac{x+12}{5}$ $+12$ then $\div 5$ INVERSES REVERSE!

← must show that way.

