

Final Review 3

Period _____

Simplify. Your answer should contain only positive exponents.

1)
$$\frac{(2x)^{-3} \cdot 2x^{-1}y^{-4}}{2yx^4}$$

2)
$$\frac{2uv \cdot u^3v^2}{(v^3)^{-2} \cdot 2u^{-2}}$$

Simplify.

3) $(4 - 4i) - (-6 + 8i)$

4) $(-5 + 2i)(7 + i)$

5) $\sqrt{80}$

6) $\sqrt{175}$

Find the inverse of each function.

7) $f(x) = 7x - 3$

8) $f(x) = \sqrt[3]{x-1} - 2$

9) $g(x) = \sqrt[3]{\frac{x-1}{2}}$

State if the given functions are inverses.

10) $f(x) = -7x - 5$
 $g(x) = \frac{-x-5}{7}$

Rewrite each equation in exponential form.

11) $\log_{12} 144 = 2$

Rewrite each equation in logarithmic form.

12) $16^2 = 256$

Solve each equation. Round your answers to the nearest ten-thousandth.

13) $16^n - 5 = 73$

14) $17^x + 8 = 60$

Solve each equation by factoring.

15) $n^2 + 3n - 10 = 0$

16) $m^2 + 8m = 0$

17) $7n^2 + 5n = 0$

18) $3x^2 - 10x + 8 = 0$

Factor each completely.

19) $9m^2 - 16$

20) $25x^2 - 40x + 16$

Find all roots.

21) $x^3 - 3x^2 - 4x = 0$

22) $x^3 + 2x^2 + 5x = 0$

Simplify each expression.

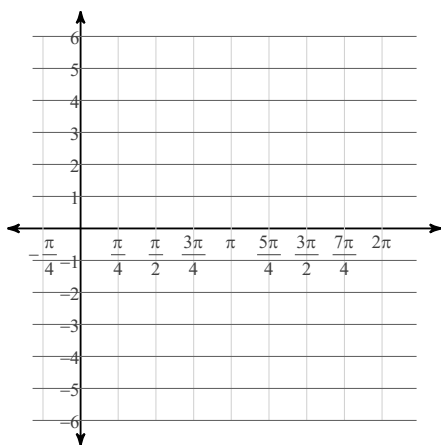
23) $\frac{v-3}{v^2-9}$

24) $\frac{x+6}{3x} \cdot \frac{3x^2-6x}{x^2+4x-12}$

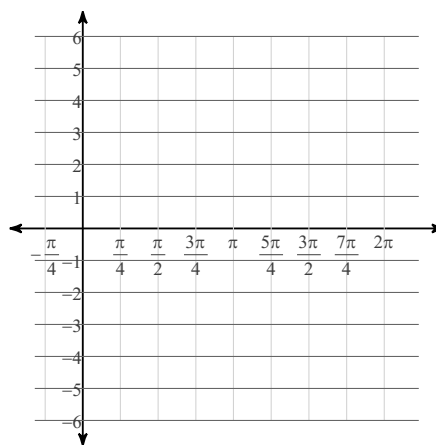
25) $\frac{1}{7a^2} \div \frac{2a-14}{a^2-2a-35}$

Graph each function using radians.

26) $y = 4\cos 2\theta + 1$

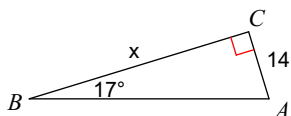


27) $y = 3\sin 4\theta - 1$

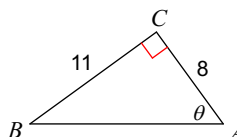


Find the measure of each side indicated. Round to the nearest tenth.

28)

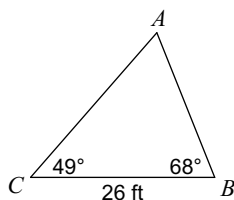


29)

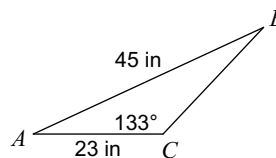


Find each measurement indicated. Round your answers to the nearest tenth.

30) Find AB



31) Find $m\angle B$



Perform the indicated operation.

32) $f(n) = 4n - 2$
 $g(n) = n^3 + 3n$
Find $f(n) + g(n)$

33) $f(n) = 3n + 3$
 $g(n) = 4n - 1$
Find $f(n) - g(n)$

34) $g(x) = -4x - 4$
 $h(x) = x - 1$
Find $g(x) \cdot h(x)$

35) $g(x) = 2x - 4$
 $h(x) = 4x + 3$
Find $g(h(x))$

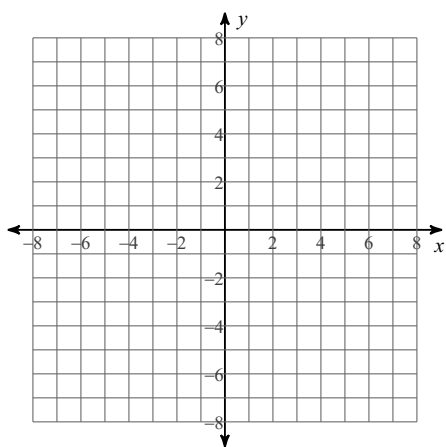
State if each scenario involves a permutation or a combination. Then find the number of possibilities.

36) A group of 35 people are going to run a race. The top three runners earn gold, silver, and bronze medals.

37) A team of 17 lacrosse players needs to choose two players to refill the water cooler.

Show long division and graph.

38)



$$x + 3\sqrt{x^3 + 4x^2 - 17x - 60}$$

Factor each. One root has been given.

39) $x^4 - 11x^3 + 37x^2 - 19x - 68 = 0$; $4 + i$

Final Review 3

Simplify. Your answer should contain only positive exponents.

1) $\frac{(2x)^{-3} \cdot 2x^{-1}y^{-4}}{2yx^4}$

Handwritten work shows the expression with arrows pointing to the exponents. Below it, the simplified form is shown as $\frac{1}{8x^8y^5}$.

2) $\frac{2uv \cdot u^3v^2}{(v^3)^{-2} \cdot 2u^{-2}}$

Simplify.

3) $(4 - 4i) - (-6 + 8i)$

Handwritten work shows the subtraction: $4 - 4i + 6 - 8i$, resulting in $10 - 12i$.

4) $(-5 + 2i)(7 + i)$

Handwritten work shows the FOIL method: $-35 - 5i + 14i + 2i^2$, which simplifies to $-35 + 9i + 2(-1)$, resulting in $-37 + 9i$.

5) $\sqrt[3]{80}$

Handwritten work shows prime factorization of 80 as $2^4 \cdot 5$, and the cube root is simplified to $2 \cdot 2 \sqrt[3]{5}$.

6) $\sqrt{175}$

Find the inverse of each function. Switch & solve

7) $f(y) = 7x - 3$

Handwritten work shows the steps to solve for x: $x = \frac{y + 3}{7}$.

8) $f(x) = \sqrt[3]{x-1} - 2$

9) $g(x) = \sqrt[3]{\frac{x-1}{2}}$

State if the given functions are inverses.

10) $f(x) = -7x - 5$
 $g(x) = \frac{-x - 5}{7}$

Rewrite each equation in exponential form.

11) $\log_{12} 144 = 2$

$12^2 = 144$ ✓

Rewrite each equation in logarithmic form.

12) $16^2 = 256$

$\log_{16} 256 = 2$

Solve each equation. Round your answers to the nearest ten-thousandth.

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13) $16^n - 5 = 73$

$16^n = 78 \rightarrow \log_{16} 78 = n$
 $n = 1.5714$

14) $17^x + 8 = 60$

Solve each equation by factoring.

15) $n^2 + 3n - 10 = 0$

16) $m^2 + 8m = 0$

17) $7n^2 + 5n = 0$

$n(7n+5) = 0$
 $x = 0, -\frac{5}{7}$

$7n + 5 = 0$
 $-5 -5$
 $7n = -5$
 $n = -\frac{5}{7}$

18) $3x^2 - 10x + 8 = 0$

$3x^2$	$-4x$
$-6x$	8

$(3x-4)(x-2)$
 $x = \frac{4}{3}, 2$

Factor each completely.

19) $9m^2 - 16$

20) $25x^2 - 40x + 16 = 0$

$(5x)^2 - 4(5x) + 4^2$
 $(5x - 4)(5x - 4)$
 $(5x - 4)^2$

Find all roots.

21) $x^3 - 3x^2 - 4x = 0$

22) $x^3 + 2x^2 + 5x = 0$

$x(x^2 + 2x + 5)$ ~~CANT~~
 $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$
 $x = \frac{-2 \pm \sqrt{2^2 - 4(1)(5)}}{2(1)}$
 $= \frac{-2 \pm \sqrt{4 - 20}}{2}$
 $= \frac{-2 \pm \sqrt{-16}}{2}$
 $= \frac{-2 \pm 4i}{2}$
 $= -1 \pm 2i$
 $0, -1 + 2i, -1 - 2i$

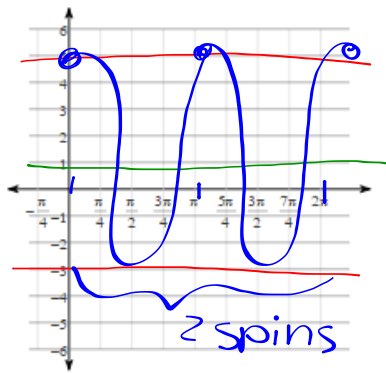
Simplify each expression.

23) $\frac{v-3}{v^2-9} \rightarrow \frac{\cancel{v-3}}{(x+3)\cancel{(x-3)}} \cdot \frac{1}{x+3}$ 24) $\frac{x+6}{3x} \cdot \frac{3x^2-6x}{x^2+4x-12}$

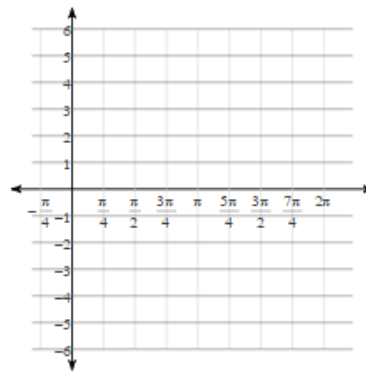
25) $\frac{1}{7a^2} \div \frac{2a-14}{a^2-2a-35}$

Graph each function using radians.

26) $y = 4\cos 2\theta + 1$

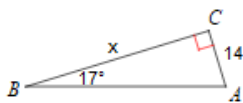


27) $y = 3\sin 4\theta - 1$



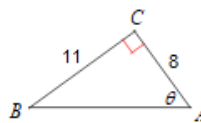
Find the measure of each side indicated. Round to the nearest tenth.

28)



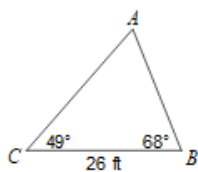
Find the measure of each angle indicated. Round to the nearest tenth.

29)

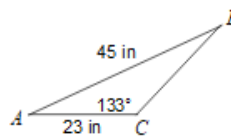


Find each measurement indicated. Round your answers to the nearest tenth.

30) Find AB



31) Find $m\angle B$



Perform the indicated operation.

32) $f(n) = 4n - 2$
 $g(n) = n^3 + 3n$
 Find $f(n) + g(n)$

33) $f(n) = 3n + 3$
 $g(n) = 4n - 1$
 Find $f(n) - g(n)$

34) $g(x) = -4x - 4$
 $h(x) = x - 1$
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35) $g(x) = 2x - 4$
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 Find $g(h(x))$

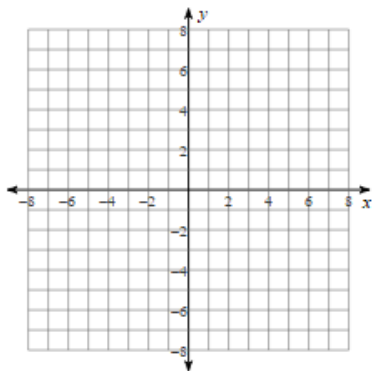
State if each scenario involves a permutation or a combination. Then find the number of possibilities.

36) A group of 35 people are going to run a race. The top three runners earn gold, silver, and bronze medals.

37) A team of 17 lacrosse players needs to choose two players to refill the water cooler.

Show long division and graph.

38)



Factor each. One root has been given.

39) $x^4 - 11x^3 + 37x^2 - 19x - 68 = 0$; $4 + i$
 on next page

$$x + 3\sqrt{x^3 + 4x^2 - 17x - 60}$$

$x^4 - 11x^3 + 37x^2 - 19x - 68$, $(4+i)$ Using $(4-i)$

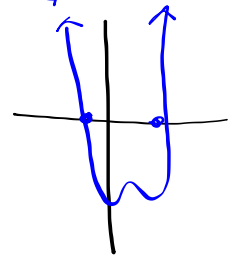
$$\begin{array}{r}
 x^2 - 3x - 4 \\
 \hline
 x^4 - 11x^3 + 37x^2 - 19x - 68 \\
 -x^4 + 8x^3 - 17x^2 \\
 \hline
 3x^3 + 20x^2 - 19x - 68 \\
 -3x^3 + 9x^2 - 12x + 12 \\
 \hline
 11x^2 - 7x - 56 \\
 -11x^2 + 33x - 44 \\
 \hline
 26x - 12 \\
 -26x + 52 \\
 \hline
 40
 \end{array}$$

$(x - 4 + i)(x - 4 - i)$

x	x^2	$-4x$	$-xi$
-4	$-4x$	16	$4i$
i	xi	$-4i$	1

$\frac{-4}{-3}$

$(x^2 - 8x + 17)$ $-i^2 = -(-1) = 1$
 $(x+1)(x-4)(x-4+i)(x-4-i)$ NO TOUCH



Perform the indicated operation.

32) $f(n) = 4n - 2$
 $g(n) = n^3 + 3n$
 Find $f(n) + g(n)$
 $n^3 + 7n - 2$

33) $f(n) = 3n + 3$
 $g(n) = 4n - 1$
 Find $f(n) - g(n)$
 $-n + 4$

34) $g(x) = -4x - 4$
 $h(x) = x - 1$
 Find $g(x) \cdot h(x)$
 $-4x^2 + 4$

35) $g(x) = 2x - 4$
 $h(x) = 4x + 3$
 Find $g(h(x))$
 $8x + 2$

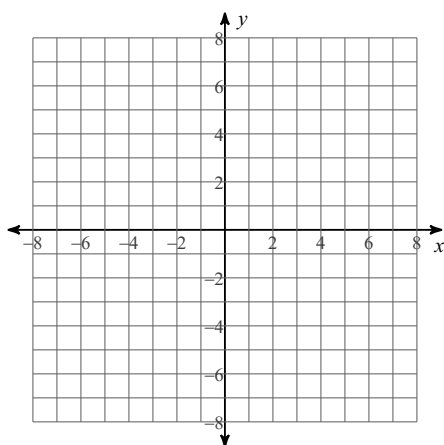
State if each scenario involves a permutation or a combination. Then find the number of possibilities.

36) A group of 35 people are going to run a race. The top three runners earn gold, silver, and bronze medals.
Permutation; 39,270

37) A team of 17 lacrosse players needs to choose two players to refill the water cooler.
Combination; 136

Show long division and graph.

38)



$x + 3\sqrt{x^3 + 4x^2 - 17x - 60}$

Factor each. One root has been given.

39) $x^4 - 11x^3 + 37x^2 - 19x - 68 = 0$; $4 + i$
 $(x + 1)(x - 4)(x^2 - 8x + 17) = 0$

Final Review 3

Period _____

Simplify. Your answer should contain only positive exponents.

1)
$$\frac{(2x)^{-3} \cdot 2x^{-1}y^{-4}}{2yx^4}$$

$$\frac{1}{8x^8y^5}$$

2)
$$\frac{2uv \cdot u^3v^2}{(v^3)^{-2} \cdot 2u^{-2}}$$

$$v^9u^6$$

Simplify.

3) $(4 - 4i) - (-6 + 8i)$

$$10 - 12i$$

4) $(-5 + 2i)(7 + i)$

$$-37 + 9i$$

5) $\sqrt{80}$

$$4\sqrt{5}$$

6) $\sqrt{175}$

$$5\sqrt{7}$$

Find the inverse of each function.

7) $f(x) = 7x - 3$

$$f^{-1}(x) = \frac{1}{7}x + \frac{3}{7}$$

8) $f(x) = \sqrt[3]{x-1} - 2$

$$f^{-1}(x) = (x+2)^3 + 1$$

9) $g(x) = \sqrt[3]{\frac{x-1}{2}}$

$$g^{-1}(x) = 2x^3 + 1$$

State if the given functions are inverses.

10) $f(x) = -7x - 5$

$$g(x) = \frac{-x-5}{7}$$

Yes

Rewrite each equation in exponential form.

11) $\log_{12} 144 = 2$

$12^2 = 144$

Rewrite each equation in logarithmic form.

12) $16^2 = 256$

$\log_{16} 256 = 2$

Solve each equation. Round your answers to the nearest ten-thousandth.

13) $16^n - 5 = 73$

1.5714

14) $17^x + 8 = 60$

1.3946

Solve each equation by factoring.

15) $n^2 + 3n - 10 = 0$

$\{2, -5\}$

16) $m^2 + 8m = 0$

$\{-8, 0\}$

17) $7n^2 + 5n = 0$

$\left\{-\frac{5}{7}, 0\right\}$

18) $3x^2 - 10x + 8 = 0$

$\left\{\frac{4}{3}, 2\right\}$

Factor each completely.

19) $9m^2 - 16$

$(3m + 4)(3m - 4)$

20) $25x^2 - 40x + 16$

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$\{0, -1, 4\}$

22) $x^3 + 2x^2 + 5x = 0$

$\{0, -1 + 2i, -1 - 2i\}$

Simplify each expression.

$$23) \frac{v-3}{v^2-9}$$

$$\frac{1}{v+3}$$

$$24) \frac{x+6}{3x} \cdot \frac{3x^2-6x}{x^2+4x-12}$$

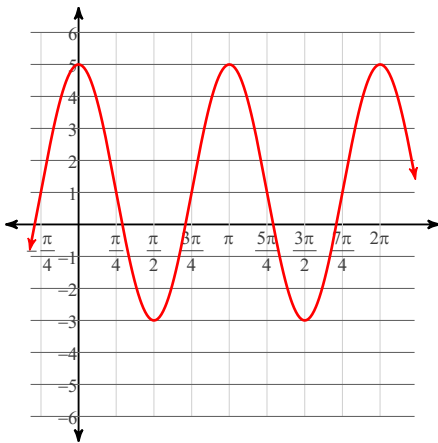
$$1$$

$$25) \frac{1}{7a^2} \div \frac{2a-14}{a^2-2a-35}$$

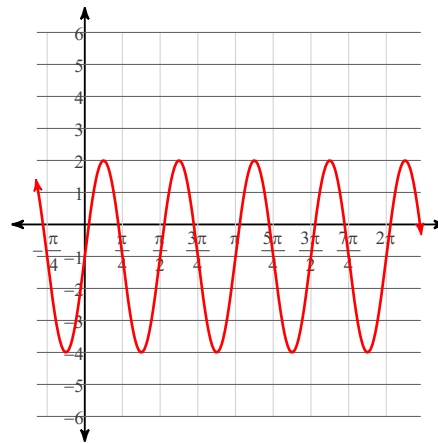
$$\frac{a+5}{14a^2}$$

Graph each function using radians.

$$26) y = 4\cos 2\theta + 1$$

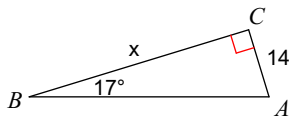


$$27) y = 3\sin 4\theta - 1$$



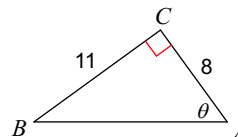
Find the measure of each side indicated. Round to the nearest tenth.

28)



45.8

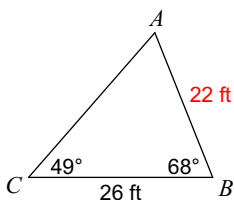
29)



54°

Find each measurement indicated. Round your answers to the nearest tenth.

30) Find AB



31) Find $m\angle B$

